Enthalpy Part 2

Energy

Enthalpy

The strength of a covalent bond is measured by its bond dissociation energy, that is, the amount of energy required to break that particular bond in a mole of molecules. Multiple bonds are stronger than single bonds between the same atoms. The enthalpy of a reaction can be estimated based on the energy input required to break bonds and the energy released when new bonds are formed. For ionic bonds, the lattice energy is the energy required to separate one mole of a compound into its gas phase ions. Lattice energy increases for ions with higher charges and shorter distances between ions. Lattice energies are often calculated using the Born-Haber cycle, a thermochemical cycle including all of the energetic steps involved in converting elements into an ionic compound.

Learning Objectives

By the end of this section, you will be able to:

- Describe the energetics of covalent and ionic bond formation and breakage
- Use the Born-Haber cycle to compute lattice energies for ionic compounds
- Use average covalent bond energies to estimate enthalpies of reaction

A bond's strength describes how strongly each atom is joined to another atom, and therefore how much energy is required to break the bond between the two atoms.

It is essential to remember that energy must be added to break chemical bonds (an endothermic process), whereas forming chemical bonds releases energy (an exothermic process). In the case of H₂, the covalent bond is very strong; a large amount of energy, 436 kJ, must be added to break the bonds in one mole of hydrogen molecules and cause the atoms to separate:

$$H_2(g) \rightarrow 2H(g)$$
 bond energy = 436 kJ

Conversely, the same amount of energy is released when one mole of H₂ molecules forms from two moles of H atoms:

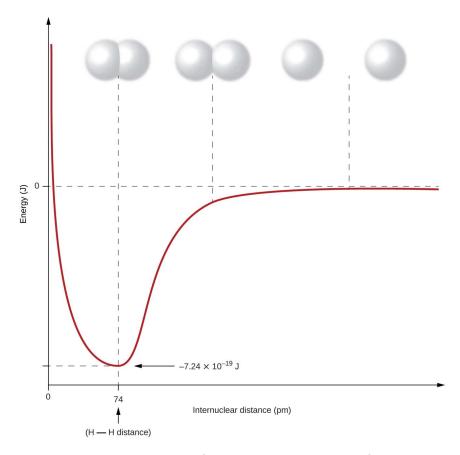
$$2H(g) \rightarrow H_2(g)$$
 bond energy = -436 kJ

Bond Strength: Covalent Bonds

Stable molecules exist because covalent bonds hold the atoms together. We measure the strength of a covalent bond by the energy required to break it, that is, the energy necessary to separate the bonded atoms. Separating any pair of bonded atoms requires energy (see <u>Figure 38.1</u>). The stronger a bond, the greater the energy required to break it.

Figure 38.1

The potential energy of two separate hydrogen atoms (right) decreases as they approach each other, and the single electrons on each atom are shared to form a covalent bond. The bond length is the internuclear distance at which the lowest potential energy is achieved.



The energy required to break a specific covalent bond in one mole of gaseous molecules is called the bond energy or the bond dissociation energy. The bond energy for a diatomic molecule, D_{X-Y} , is defined as the standard enthalpy change for the endothermic reaction:

$$XY(g) \longrightarrow X(g) + Y(g)$$
 $D_{X-Y} = \Delta H^{\circ}$

For example, the bond energy of the pure covalent H-H bond, D $_{H-H}$, is 436 kJ per mole of H-H bonds broken:

$$H_2(g) \rightarrow 2H(g)$$
 $D_{H-H} = \Delta H^\circ = 436 \text{ kJ}$

Molecules with three or more atoms have two or more bonds. The sum of all bond energies in such a molecule is equal to the standard enthalpy change for the endothermic reaction that breaks all the bonds in the molecule. For example, the sum of the four C-H bond energies in CH₄, 1660 kJ, is equal to the standard enthalpy change of the reaction:

$$H \longrightarrow H$$
 $H \longrightarrow C(g) \longrightarrow C(g) + 4H$
 H

The average C-H bond energy, D_{C-H} , is 1660/4 = 415 kJ/mol because there are four moles of C-H bonds broken per mole of the reaction. Although the four C-H bonds are equivalent in the original molecule, they do not each require the same energy to break; once the first bond is broken (which requires 439 kJ/mol), the remaining bonds are easier to break. The 415 kJ/mol value is the average, not the exact value required to break any one bond.

The strength of a bond between two atoms increases as the number of electron pairs in the bond increases. Generally, as the bond strength increases, the bond length decreases. Thus, we find that triple bonds are stronger and shorter than double bonds between the same two atoms; likewise, double bonds are stronger and shorter than single bonds between the same two atoms. Average bond energies for some common bonds appear in <u>Table 38.1</u>, and a comparison of bond lengths and bond strengths for some common bonds appears in <u>Table 38.2</u>. When one atom bonds to various atoms in a group, the bond strength typically decreases as we move down the group. For example, C-F is 439 kJ/mol, C-Cl is 330 kJ/mol, and C-Br is 275 kJ/mol.

Table 38.1Bond Energies (kJ/mol)

Bond I	Bond Energy	Bond	Bond Energy	Bond	Bond Energy
H-H	436	C-S	260	F-CI	255
H-C	415	C-CI	330	F-Br	235
H-N	390	C-Br	275	Si-Si	230
H-0	464	C-I	240	Si-P	215
H-F	569	N-N	160	Si-S	225
H-Si	395	N=N	418	Si-Cl	359
H-P :	320	N≡N	946	Si-Br	290
H-S	340	N-0	200	Si-I	215
H-Cl	432	N-F	270	P-P	215
H-Br	370	N-P	210	P-S	230
H-I :	295	N-CI	200	P-CI	330

Bond	Bond Energy	Bond	Bond Energy	Bond	Bond Energy
C-C	345	N-Br	245	P-Br	270
C=C	611	0-0	140	P-I	215
C≡C	837	O=O	498	S-S	215
C-N	290	0-F	160	S-CI	250
C=N	615	0-Si	370	S-Br	215
C≡N	891	0-P	350	CI-CI	243
C-O	350	O-CI	205	Cl-Br	220
C=O	741	0-1	200	CI-I	210
C≡O	1080	F-F	160	Br-Br	190
C-F	439	F-Si	540	Br-I	180
C-Si	360	F-P	489	1-1	150
C-P	265	F-S	285		

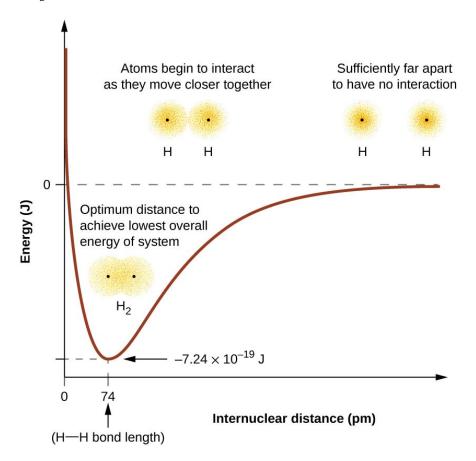
Table 38.2Average Bond Lengths and Bond Energies for Some Common Bonds

Bond	Bond Length (Å)	Bond Energy (kJ/mol)
C-C	1.54	345
C=C	1.34	611
C≡C	1.20	837
C-N	1.43	290
C=N	1.38	615
C≡N	1.16	891
C-O	1.43	350
C=O	1.23	741
C≡O	1.13	1080

The bond energy is the difference between the energy minimum (which occurs at the bond distance) and the energy of the two separated atoms. This is the quantity of energy released when the bond is formed. Conversely, the same amount of energy is required to break the bond. For the H_2 molecule shown in Figure 38.2, at the bond distance of 74 pm the system is 7.24×10^{-19} J lower in energy than the two separated hydrogen atoms. This may seem like a small number. However, as we will learn in more detail later, bond energies are often discussed on a per-mole basis. For example, it requires 7.24×10^{-19} J to break one H–H bond, but it takes 4.36×10^5 J to break 1 mole of H–H bonds. A comparison of some bond lengths and energies is shown in Figure 38.2 and Table 38.1. We can find many of these bonds in a variety of molecules, and this table provides average values. For example, breaking the first C–H bond in CH₄ requires 439.3 kJ/mol, while breaking the first C–H bond in H–CH₂C₆H₅ (a common paint thinner) requires 375.5 kJ/mol.

Figure 38.2

(a) The interaction of two hydrogen atoms changes as a function of distance. (b) The energy of the system changes as the atoms interact. The lowest (most stable) energy occurs at a distance of 74 pm, which is the bond length observed for the H_2 molecule.



As seen in Table 38.1 and Table 38.2, an average carbon-carbon single bond is 347 kJ/mol, while in a carbon-carbon double bond, the π bond increases the bond strength by 267 kJ/mol. Adding an additional π bond causes a further increase of 225 kJ/mol. We can see a similar pattern when we compare other σ and π bonds. Thus, each individual π bond is generally weaker than a corresponding σ bond between the same two atoms. In a σ bond, there is a greater degree of orbital overlap than in a π bond.

We can use bond energies to calculate approximate enthalpy changes for reactions where enthalpies of formation are not available. Calculations of this type will also tell us whether a reaction is exothermic or endothermic. An exothermic reaction (ΔH negative, heat produced) results when the bonds in the products are stronger than the bonds in the reactants. An endothermic reaction (ΔH positive, heat absorbed) results when the bonds in the products are weaker than those in the reactants.

The enthalpy change, ΔH , for a chemical reaction is approximately equal to the sum of the energy required to break all bonds in the reactants (energy "in", positive sign) plus the energy released when all bonds are formed in the products (energy "out," negative sign). This can be expressed mathematically in the following way:

$$\Delta H = \Sigma D_{\text{bonds broken}} - \Sigma D_{\text{bonds formed}}$$

In this expression, the symbol Σ means "the sum of" and D represents the bond energy in kilojoules per mole, which is always a positive number. The bond energy is obtained from a table (like <u>Table 38.2</u>) and will depend on whether the particular bond is a single, double, or triple bond. Thus, in calculating enthalpies in this manner, it is important that we

consider the bonding in all reactants and products. Because D values are typically averages for one type of bond in many different molecules, this calculation provides a rough estimate, not an exact value, for the enthalpy of reaction.

Consider the following reaction:

$$H_2(g) + Cl_2(g) \rightarrow 2HCl(g)$$

or

$$H-H(g) + Cl-Cl(g) \rightarrow 2H-Cl(g)$$

To form two moles of HCl, one mole of H-H bonds and one mole of Cl-Cl bonds must be broken. The energy required to break these bonds is the sum of the bond energy of the H-H bond (436 kJ/mol) and the Cl-Cl bond (243 kJ/mol). During the reaction, two moles of H-Cl bonds are formed (bond energy = 432 kJ/mol), releasing 2×432 kJ; or 864 kJ. Because the bonds in the products are stronger than those in the reactants, the reaction releases more energy than it consumes:

$$\Delta H = \Sigma D_{\text{bonds broken}} - \Sigma D_{\text{bonds formed}}$$

$$\Delta H = [D_{\text{H-H}} + D_{\text{Cl-Cl}}] - 2D_{\text{H-Cl}}$$

$$= [436 + 243] - 2(432) = -185 \text{ kJ}$$

This excess energy is released as heat, so the reaction is exothermic. OpenStax's $\underline{\text{Appendix G}}$ gives a value for the standard molar enthalpy of formation of HCl(g),

$$\Delta H_{\rm f}^{\circ}$$
,

of -92.307 kJ/mol. Twice that value is -184.6 kJ, which agrees well with the answer obtained earlier for the formation of two moles of HCl.

Example 38.1

Using Bond Energies to Calculate Approximate Enthalpy Changes

Methanol, CH₃OH, may be an excellent alternative fuel. The high-temperature reaction of steam and carbon produces a mixture of the gases carbon monoxide, CO, and hydrogen, H₂, from which methanol can be produced. Using the bond energies in <u>Table 38.2</u>, calculate the approximate enthalpy change, ΔH , for the reaction here:

$$CO(g) + 2H_2(g) \rightarrow CH_3OH(g)$$

Solution

First, we need to write the Lewis structures of the reactants and the products:

From this, we see that ΔH for this reaction involves the energy required to break a C-O triple bond and two H-H single bonds, as well as the energy produced by the formation of three C-H single bonds, a C-O single bond, and an O-H single bond. We can express this as follows:

$$\Delta H = \sum D_{\text{bonds broken}} - \sum D_{\text{bonds formed}}$$

$$\Delta H = [D_{C \equiv O} + 2(D_{H-H})] - [3(D_{C-H}) + D_{C-O} + D_{O-H}]$$

Using the bond energy values in Table 38.2, we obtain:

$$\Delta H = [1080 + 2(436)] - [3(415) + 350 + 464]$$

= -107 kJ

We can compare this value to the value calculated based on

$$\Delta H_{\mathrm{f}}^{\circ}$$

data from Appendix G:

$$\Delta H = [\Delta H_{f}^{\circ} CH_{3} OH(g)] - [\Delta H_{f}^{\circ} CO(g) + 2 \times \Delta H_{f}^{\circ} H_{2}]$$

$$= [-201.0] - [-110.52 + 2 \times 0]$$

$$= -90.5 \text{ kJ}$$

Note that there is a fairly significant gap between the values calculated using the two different methods. This occurs because D values are the *average* of different bond strengths; therefore, they often give only rough agreement with other data.

Check Your Learning

Ethyl alcohol, CH₃CH₂OH, was one of the first organic chemicals deliberately synthesized by humans. It has many uses in industry, and it is the alcohol contained in alcoholic beverages. It can be obtained by the fermentation of sugar or synthesized by the hydration of ethylene in the following reaction:

Using the bond energies in Table 38.2, calculate an approximate enthalpy change, ΔH , for this reaction.

Answer

-35 kJ

Ionic Bond Strength and Lattice Energy

An ionic compound is stable because of the electrostatic attraction between its positive and negative ions. The lattice energy of a compound is a measure of the strength of this attraction. The lattice energy ($\Delta H_{\text{lattice}}$) of an ionic compound is defined as the energy required to separate one mole of the solid into its component gaseous ions. For the ionic solid MX, the lattice energy is the enthalpy change of the process:

$$MX(s) \rightarrow M^{n+}(g) + X^{n-}(g)$$
 $\Delta H_{lattice}$

Note that we are using the convention where the ionic solid is separated into ions, so our lattice energies will be *endothermic* (positive values). Some texts use the equivalent but opposite convention, defining lattice energy as the energy released when separate ions combine to form a lattice and giving negative (exothermic) values. Thus, if you are looking up lattice energies in another reference, be certain to check which definition is being used. In both cases, a larger magnitude for lattice energy indicates a more stable ionic compound. For sodium chloride, $\Delta H_{\text{lattice}} = 769 \text{ kJ}$. Thus, it requires 769 kJ to separate one mole of solid NaCl into gaseous Na⁺ and Cl⁻ ions. When one mole each of gaseous Na⁺ and Cl⁻ ions form solid NaCl, 769 kJ of heat is released.

The lattice energy $\Delta H_{\text{lattice}}$ of an ionic crystal can be expressed by the following equation (derived from Coulomb's law, governing the forces between electric charges):

$$\Delta H_{\text{lattice}} = \frac{C(Z^+)(Z^-)}{R_0}$$

in which C is a constant that depends on the type of crystal structure; Z^+ and Z^- are the charges on the ions; and R_o is the interionic distance (the sum of the radii of the positive and negative ions). Thus, the lattice energy of an ionic crystal increases rapidly as the charges of the ions increase and the sizes of the ions decrease. When all other parameters are kept constant, doubling the charge of both the cation and anion quadruples the lattice energy. For example, the lattice energy of LiF (Z^+ and Z^- = 1) is 1023 kJ/mol, whereas that of MgO (Z^+ and Z^- = 2) is 3900 kJ/mol (R_o is nearly the same —about 200 pm for both compounds).

Different interatomic distances produce different lattice energies. For example, we can compare the lattice energy of MgF₂ (2957 kJ/mol) to that of MgI₂ (2327 kJ/mol) to observe the effect on lattice energy of the smaller ionic size of F⁻ as compared to I⁻.

Example 38.2

Lattice Energy Comparisons

The precious gem ruby is aluminum oxide, Al_2O_3 , containing traces of Cr^{3+} . The compound Al_2Se_3 is used in the fabrication of some semiconductor devices. Which has the larger lattice energy, Al_2O_3 or Al_2Se_3 ?

Solution

In these two ionic compounds, the charges Z^+ and Z^- are the same, so the difference in lattice energy will depend upon R_o . The O^{2^-} ion is smaller than the Se^{2^-} ion. Thus, Al_2O_3 would have a shorter interionic distance than Al_2Se_3 , and Al_2O_3 would have the larger lattice energy.

Check Your Learning

Zinc oxide, ZnO, is a very effective sunscreen. How would the lattice energy of ZnO compare to that of NaCl?

Answer

ZnO would have the larger lattice energy because the Z values of both the cation and the anion in ZnO are greater, and the interionic distance of ZnO is smaller than that of NaCl.

The Born-Haber Cycle

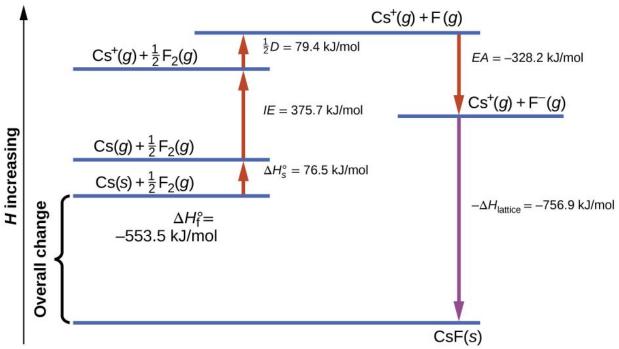
It is not possible to measure lattice energies directly. However, the lattice energy can be calculated using the equation given in the previous section or by using a thermochemical cycle. The Born-Haber cycle is an application of Hess's law that breaks down the formation of an ionic solid into a series of individual steps:

- $\Delta H_{\rm f}^{\circ}$, the standard enthalpy of formation of the compound
- IE, the ionization energy of the metal
- EA, the electron affinity of the nonmetal
- $\Delta H_{\rm S}$, the enthalpy of sublimation of the metal
- D, the bond dissociation energy of the nonmetal
- $\Delta H_{\text{lattice}}$, the lattice energy of the compound

Figure 38.3 diagrams the Born-Haber cycle for the formation of solid cesium fluoride.

Figure 38.3

The Born-Haber cycle shows the relative energies of each step involved in the formation of an ionic solid from the necessary elements in their reference states.



We begin with the elements in their most common states, Cs(s) and $F_2(g)$. The

$$\Delta H_{\rm s}^{\circ}$$

represents the conversion of solid cesium into a gas, and then the ionization energy converts the gaseous cesium atoms into cations. In the next step, we account for the energy required to break the F–F bond to produce fluorine atoms. Converting one mole of fluorine atoms into fluoride ions is an exothermic process, so this step gives off energy (the electron affinity) and is shown as decreasing along the *y*-axis. We now have one mole of Cs cations and one mole of F anions. These ions combine to produce solid cesium fluoride. The enthalpy change in this step is the negative of the lattice energy, so it is also an exothermic quantity. The total energy involved in this conversion is equal to the experimentally determined enthalpy of formation,

$$\Delta H_{\rm f}^{\circ}$$
,

of the compound from its elements. In this case, the overall change is exothermic.

Hess's law can also be used to show the relationship between the enthalpies of the individual steps and the enthalpy of formation. Table 38.3 shows this for cesium fluoride, CsF.

Table 38.3

Enthalpy of sublimation of Cs(s)	$C_{S}(s) \longrightarrow C_{S}(g)$	$\Delta H = \Delta H_s^{\circ} = 76.5 \text{kJ/mol}$
One-half of the bond energy of F ₂	$\frac{1}{2} \mathrm{F}_2(\mathrm{g}) \longrightarrow \mathrm{F}(\mathrm{g})$	$\Delta H = \frac{1}{2}D = 79.4 \text{kJ/mol}$
Ionization energy of $Cs(g)$	$Cs(g) \rightarrow Cs^{+}(g) + e^{-}$	$\Delta H = IE = 375.7 \text{kJ/mol}$
Electron affinity of F	$F(g) + e^- \rightarrow F^-(g)$	$\Delta H = EA = -328.2 \text{kJ/mol}$

Negative of the lattice energy of CsF(s)	$Cs^+(g) + F^-(g) \rightarrow CsF(s)$	$\Delta H = -\Delta H_{\text{lattice}} = ?$
Enthalpy of formation of CsF(s), add steps 1–5	$\Delta H = \Delta H_f^{\circ} = \Delta H_s^{\circ} + \frac{1}{2}D + IE + (EA) + (-\Delta H_{\text{lattice}})$ $C_S(s) + \frac{1}{2}F_2(g) \longrightarrow C_SF(s)$	$\Delta H = -553.5 \text{kJ/mol}$

Thus, the lattice energy can be calculated from other values. For cesium fluoride, using this data, the lattice energy is:

$$\Delta H_{\text{lattice}} = 76.5 + 79.4 + 375.7 + (-328.2) - (-553.5) = 756.9 \text{ kJ/mol}$$

The Born-Haber cycle may also be used to calculate any one of the other quantities in the equation for lattice energy, provided that the remainder is known. For example, if the relevant enthalpy of sublimation

$$\Delta H_{s}^{\circ}$$
,

ionization energy (IE), bond dissociation enthalpy (D), lattice energy $\Delta H_{\text{lattice}}$, and standard enthalpy of formation

$$\Delta H_{\mathrm{f}}^{\circ}$$

are known, the Born-Haber cycle can be used to determine the electron affinity of an atom.

Lattice energies calculated for ionic compounds are typically much higher than bond dissociation energies measured for covalent bonds. Whereas lattice energies typically fall in the range of 600–4000 kJ/mol (some even higher), covalent bond dissociation energies are typically between 150–400 kJ/mol for single bonds. Keep in mind, however, that these are not directly comparable values. For ionic compounds, lattice energies are associated with many interactions, as cations and anions pack together in an extended lattice. For covalent bonds, the bond dissociation energy is associated with the interaction of just two atoms.

Link to Supplemental Exercises

Supplemental exercises are available if you would like more practice with these concepts.

Files

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